

WHEN A MAN RUNS ALONE IT IS CALLED RACE, BUT
WHEN HE RUN WITH GOD IT IS CALLED GRACE.

MAT 112 PRACTICE QUESTIONS

- (1) Find the derivative of $y=3x^2\sin x$ (a) $2x(x\cos x+2\sin x)$ (b) $6x(x\cos x + 2\sin x)$
(c) $3x(x\cos x+2\sin x)$ (d) $6x(x\sin x + 2\cos x)$
- (2) Find the value of $\frac{\partial y}{\partial x}$ of the equation $3(x^2+y^2)^2 - 100xy$ at point (3,1) (a) $-9/13$
(b) $13/9$ (c) $9/13$ (d) $-13/9$
- (3) Find the derivative of $y= x^2\sqrt{1-x^2}$ (a) $\frac{2x(3-2x^2)}{1-x^2}$ (b) $\frac{3x(2x-4x^2)}{\sqrt{1-x^2}}$
(c) $\frac{x(2-3x^2)}{\sqrt{1-x^2}}$ (d) $\frac{x(2+3x^2)}{\sqrt{1-x^2}}$
- (4) Find the derivative of $y= \sin^3 4t$. (a) $-12\sin^2 4t\cos 4t$ (b) $3\cos 4t\sin 4t$
(c) $12\sin^2 4t\cos 4t$ (d) $-3\cos 4t\sin 4t$
- (5) If d^2y/dx^2 is greater than zero, we have a point **(a) minimum**
 (b) maximum (c) infinite (d) zero
- (6) if $y = 5x+3$, find y^{-1} (inverse of y) (a) $\frac{3-x}{5}$ (b) $\frac{1}{5x+3}$ **(c) $\frac{x-3}{5}$**
 (d) $\frac{5x-3}{2}$
- (7) Integration is the _____ of differentiation (a) power **(b) inverse**
 (c) opposite (d) factor
- (8) The formular of integration by part was derived to be? (a)
 $\int u dv = \int v du - uv$ (b) $\int u dv = uv + \int v du$ **(c) $\int u dv = uv - \int v du$**
 (d) $\int v du = uv - \int u dv$
- (9) $\int_0^1 x(x^2+1)^3 dx$ (a) $-8/15$ (b) $15/7$ (c) $-15/8$ **(d) $15/8$**

(10) $\int \sin^2 3x \cos 3x dx$ (a) $-1/3 \sin^2 3x (3 \sin 3x) + c$ (b) $1/9 \sin^3 3x + c$ (c) $-1/9 \sin^3 3x + c$ (d) $2 \cos 3x \sin 3x + c$

(1) $Y = \tan x, \frac{dy}{dx} = ?$ (a) $\tan^2 x$ (b) $\sin^2 x$ (c) $-\sec x$ (d) $\sec^2 x$

(2) $\lim_{x \rightarrow 3} \frac{x^2 - 9}{x - 3}$ (a) infinity (b) 0 (c) 3 (d) 6

(3) Differentiate $x \sin x \cos x$ (a) $x \cos x - \sin x$ (b) $\cos x - \sin x$ (c) $x \cos x$ (d) $x \cos + 2 \sin x$

(4) The gradient of the curve

$4x^2 + 2x + 3$ at $x = -2$ is (a) 15 (b) -15 (c) -14 (d) none of the above

(5) $\int 1/x dx$ is (a) $-x + c$ (b) $-1/x^2$ (c) $\ln x + c$ (d) $x^2 + c$

(6) find $\frac{dy}{dx}$ if $y = \frac{x^2}{2x+1}$ (a) $\frac{2x(x+1)}{(2x+1)}$ (b) $\frac{4x(x+1)}{(2x+1)^2}$ (c) $\frac{6x^2+2x}{(2x+1)^2}$ (d) $\frac{2x(x+1)}{(2x+1)^2}$

(7) differentiate y

$= (2x^2 + 3x - 1)^3$ (a) $3(2x^2 + 3x - 1)^2$ (b) $12x + 9$ (c) $(2x^2 + 3x - 1)^2(12x + 9)$ (d) $-3(2x^2 + 3x - 1)^2(4x + 3)$

(8) find $\frac{dy}{dx}$ if $y = \sin^2(x^2 + 1)$ (a) $4x \sin(x^2 + 1)$ (b) $2 \sin(x^2 + 1)$ (c) $(2x + 1) \cos^2(x^2 + 1)$ (d) no answer

(9) differentiate $y = \cos x$ (a) $\frac{1}{\sqrt{1-x^2}}$ (b) $\frac{-1}{\sqrt{1-x^2}}$ (c) $\frac{1}{1-x^2}$ (d) $\frac{-1}{1-x^2}$

(10) find $\frac{dy}{dx}$ if $y = \sin^{-1} 4x$ (a) $\frac{1}{\sqrt{1-16x^2}}$ (b) $\frac{-1}{\sqrt{1-16x^2}}$ (c) $\frac{4}{\sqrt{1-16x^2}}$ (d) $\frac{-4}{1-16x^2}$

(11)

what is the equation of the curve of gradient $8x + 2$ at point $(1, -2)$? (a) $8x^2 + 2x + 8$ (b) $4x^2 - 2x - 8$ (c) $2x^2 + 2x + 8$ (d) $2x^2 + x - 4$

(12) $\lim_{x \rightarrow 0} \frac{\sin x}{x}$ is (a) infinity (b) 1 (c) -1 (d) zero

(13) $\lim_{x \rightarrow 0} \frac{\cos x}{x}$ is (a) infinity (b) 1 (c) -1 (d) zero

(14) $\lim_{x \rightarrow 3} e^{3x}$ is (a) e^6 (b) $3e^9$ (c) e^9 (d) e^9

(15) $\lim_{x \rightarrow \infty} \frac{4x^4 + 3x^3 + 9x^2 + 2}{3x^4}$ is (a) infinity (b) zero (c) (d) $4/3$

(16) $\lim_{x \rightarrow -1} \left(\frac{x^2 + 2x + 1}{x^2 + 3x + 2} \right)$ (a) infinity (b) zero (c) 1 (d) -1

(17) $\lim_{x \rightarrow \frac{\pi}{4}} (3x - \tan x)$ (a) $1 - \frac{3\pi}{4}$ (b) $\frac{3\pi}{4} - 1$ (c) $\tan \frac{\pi}{4} - \frac{3\pi}{4}$ (d) no answer

(18)

$\int \frac{7x+8}{2x^2+11x+5} dx$ (a) $(x+5) \ln(3+x) + c$ (b) $3 \ln(x+5) + \frac{1}{2} \ln(2x+1) + c$ (c) no answer (d) $3 \ln(7x+8) + \frac{1}{2} \ln(2x+1) + c$

(19) $\int (3x+2)^4 dx$ (a) $4(3x+2)^3 + c$ (b) $12(3x+2)^3 + c$ (c) $\frac{(3x+2)^5}{15} + c$ (d) no answer

(20) $\int \sin^2 x dx$ (a) $\frac{1}{2} - \cos x + c$ (b) $2 \sin^2 x \cos x + c$ (c) $\sin x + x + c$ (d) no answer

(21)

differentiate $x^3 \cos x$ (a) $3x^2 \cos x - x^3 \sin x$ (b) $3x^2 \sin x + x^3 \cos x$ (c) $3x^2 \cos x + x \sin x$ (d) $3x^2 \sin x - x^3 \cos x$

(22) find the derivative of $\log(\sin x^2)$ with respect to x (a) $\frac{2}{x} \cos x^2$ (b) $2x \cot x^2$ (c) $\frac{2}{x} (\log_{10} \cos x^2)$

(d) $2x \log(\cos x^2)$

(23) evaluate $\lim_{x \rightarrow 3} \frac{x^3 - 24x}{x^2 - 9}$ (a) 0 (b) 1 (c) 2 (d) infinity

(24) integrate $\frac{\cos x}{5 + \sin x}$ (a) $\ln(3 + \sin x) + c$ (b) $\frac{5}{(5 + \sin x)^2} + c$ (c) $\ln(5 + \sin x) + c$ (d) $\frac{1}{5} \ln(5 + \cos x) + c$

(25) $\lim_{x \rightarrow 1} \frac{\ln x}{x-1}$ (a) 1 (b) 0 (c) ∞ (d) $\frac{1}{2}$

(26) Evaluate $\int_0^{\infty} e^{-4x} dx$ (a) $\frac{1}{2}$ (b) $\frac{1}{4}$ (c) $\frac{-1}{2}$ (d) $\frac{-1}{4}$

(27) find $\int \frac{1}{\sqrt{25-9x^2}} dx$ (a) $\frac{1}{3} \sin^{-1} \left(\frac{3x}{5} \right)$ (b) $\frac{1}{5} \sin^{-1} \left(\frac{3x}{5} \right)$ (c) $\frac{1}{3} \cos^{-1} \left(\frac{3x}{5} \right)$ (d) $\frac{1}{15} \sin^{-1} \left(\frac{3x}{5} \right)$

(28) $y = t^3 \sin t + \cos 3t$ $x = 2t - \cos t$ find $\frac{dy}{dx}$ (a) $\frac{t^3 \cos t + 3t^2 - 3 \sin 3t}{2 + \sin t}$ (b) $\frac{t^2 \cos t - 3t^2 \sin t + 3 \cos 3t}{2 + \sin t}$

(29) if $\frac{d^2y}{dx^2} < 0, \dots \dots$ point occur. (a) minimum (b) maximum (c) dormant (d) mini - maximum

(30) if $x^2 + y^2 = \sin x$ find $\frac{dy}{dx}$ at point (0,2) (a) $\frac{-1}{4}$ (b) $\frac{1}{4}$ (c) 4 (d) -4

(31) find $\frac{dy}{dx}$ when $x^2 y + y^2 = \sin x$ at point (0,3) (a) $\frac{1}{9}$ (b) $\frac{-1}{9}$ (c) $\frac{1}{6}$ (d) $\frac{-1}{6}$

(32)

determine the value of $\frac{d^2y}{dx^2}$ at the stationary point of the equation $y = x^3 + 2x^2 + x + 3$ (a) -6 (b) 4 (c) -4 (d) 6

(33)

find the area of the region under the line $y = 2x + 1$ over the interval $1 \leq x \leq 3$ (a) -12 (b) 11 (c) 9 (d) 10

(34) reduction formular is derived from ... (a) differentiation

(b) integration by part (c) quocient rule (d) explicit rule

(35) find the area of the curve $y = \cos x$ between $x = 0$ and $x = \pi/2$ (a) 1 (b) -1 (c) 2 (d) $\frac{1}{2}$

(36)

find the volume generated when the plane figure bounded by $y = 5\cos 2x$, the x -axis and ordinate at $x = 0$ and $x =$

$\frac{\pi}{4}$, rotates about the x -axis through a complete revolution. (a) $\frac{8\pi^2}{25}$ (b) $\frac{25}{8}\pi^2$ (c) $\frac{27}{8}\pi^3$ (d) $\frac{8}{27}\pi^2$

(37) if $y = \frac{u}{v}$, $\frac{dy}{dx}$ with respect to u, v is given as: (a) $u \frac{dv}{dx} - v \frac{du}{dx}$ (b) $v \frac{du}{dx} - u \frac{dv}{dx}$ (c) $\frac{v \frac{du}{dx} - u \frac{dv}{dx}}{v^2}$ (d) $\frac{u \frac{dv}{dx}}{v^2}$

(38) if $y = \sin p$, $\frac{d^2y}{dp^2}$ is? (a) $\sin^2 p$ (b) $-\sin p$ (c) $\cos p$ (d) $-\cos p$

(39) if $y = \sin^{-1} 4x$, $\frac{dy}{dx}$ is? (a) $\frac{4}{\sqrt{1-4x^2}}$ (b) $\frac{-4}{\sqrt{1+4x^2}}$ (c) $\frac{4}{\sqrt{1-16x^2}}$ (d) $\frac{4}{\sqrt{1+16x}}$

(40) $\int x^4 dx$ (a) $4x^3 + c$ (b) $\frac{4x^5}{5} + c$ (c) $\frac{x^5}{5} + c$ (d) $\frac{5x^4}{4}$