

PHY 124 SOLUTIONS

FOR

PHARMACY STUDENTS

MADE EASY

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CHAPTER ONE EXERCISE

1. $Q_1 = +3\mu\text{c}$, $Q_2 = +5\mu\text{c}$, $r = 0.3\text{m}$

Calculate the net force

$$f = \frac{KQ_1Q_2}{r^2} = \frac{9 \times 10^9 \times 3 \times 5 \times 10^{-12}}{0.3} [10^{-6} \times 10^{-6} = 10^{-12}]$$

$F = 1.5\text{M}$ (Like charges Repel, Hence the force is Repulsive.)

2. Same procedure $Q_1 = Q_2 = +5\mu\text{c} = 5 \times 10^{-6}\text{c}$
 $r = 0.05\text{m}$,

$$f = \frac{KQ_1Q_2}{r^2} = \frac{9 \times 10^9 \times 3 \times 5 \times 10^{-6}}{0.05}$$

$$F = 90\text{N}$$

3. force due to gravity (fg) Electrostatic force (i.e)

$$f_g = f_e \text{-----} Mx(g) = \frac{KQ^2}{r^2} r^2 = \frac{KQ^2}{M_e x g}$$

$$r = \sqrt{\frac{k}{m_e g}} = 1.6 \times 10^{-19} \sqrt{\frac{9 \times 10^9}{9.1024 \times 10 \times 9.8}}$$

$$r = 5.03\text{m}$$

4. $r = 0.3\text{m}$, $F = 2.30 \times 10^{-22}\text{N}$

$$\text{using } f = \frac{KQ^2}{r^2}, Q^2 = \frac{fr^2}{K}, Q = \sqrt{\frac{fr^2}{K}}$$

$$Q = 0.3 \sqrt{\frac{2.3 \times 10^{-22}}{9 \times 10^9}} = 4.796 \times 10^{-17}\text{c}$$

But $Q = ne, n = \frac{Q}{e} = \frac{4.796 \times 10^{-17}}{1.6 \times 10^{-19}} = 2199.7 \dots \text{electrons}$

$n = 300$ electrons.

5. A) conventionally: $F_R = -F_x$
 -ve because of direction

$$f_x = \frac{KQ_1Q_2}{r^2} = \frac{9 \times 10^9 \times 2 \times 3 \times 10^{-12}}{(0.15)^2} = 2.4$$

$$f_y = \frac{KQ_1Q_2}{r^2} = \frac{9 \times 10^9 \times 2 \times 4 \times 10^{-12}}{(0.1)^2} = 7.2$$

But $|F_R| = |F_x| + |F_y|$ as stated above

$$|F_R| = (-2.4)i + (7.2)j; N$$

$$\text{Magnitude of } F_R \text{ i.e. } F_R^2 = f_x^2 + f_y^2$$

$$F_R = \sqrt{(-2.4)^2 + (7.2)^2} = 7.59 = 7.6 N$$

c. The angle that F_R makes with the +ve x - axis is 2

but $2 = 180 - \theta$ (angle on a straight line)

$$\theta = \tan^{-1} \left\{ \frac{f_y}{f_x} \right\} = \tan^{-1} \left[\frac{7.2}{2.4} \right], \theta = 71.57^\circ$$

$$2 = 180 - \theta = 180 - 71.57, 2 = 108$$

CHAPTER TWO EXERCISES

$$Q = 1.6 \times 10^{-19} \text{ C}, E = 120,000 \text{ V m}^{-1} = 120,000 \text{ N / C}$$

$$r = 20 \text{ mm} = 0.02 \text{ m}, m = 9.1 \times 10^{-31} \text{ kg}$$

$$f_e = f_g$$

$$1. \quad f_e = qE = 120,000 \times 1.6 \times 10^{-19} = 1.92 \times 10^{-14} \text{ N}$$

$$f = Ma, a = \frac{f}{m} = \frac{1.92 \times 10^{-14}}{9.109 \times 10^{-31}} = 2.11 \times 10^{16} \text{ ms}^{-2}$$

$$S = ut + \frac{1}{2}gt^2$$

But $u = 0$ (travels from rest)

$$S = \frac{1}{2}gt^2, t = \sqrt{\frac{2S}{g}} = \sqrt{\frac{2 \times 0.02}{2 \times 10^{16}}} = 1.377 \times 10^{-9} \text{ s}$$

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$$3a) E = \frac{f}{Q} = \frac{KQ}{r^2} = \frac{9 \times 10^9 \times 3 \times 10^{10}}{0.02^2} E = 6750 \\ 6.8 \times 10^3 \text{ N/C}$$

B) $E = 20\%$ of original value E_0

$$E = \frac{20}{100} \times E_0 = \frac{KQ}{r^2} = \frac{2}{10} E_0 = \frac{9 \times 10^9 \times 3 \times 10^{10}}{r^2}$$

$$= \frac{2}{10} \times 6.8 \times 10^3 r^2 = 1.985 \times 10^{-3} = 0.044 \text{ m} = 4 \text{ cm}$$

$$\text{Moment} = 6.2 \times 10^{-3} \text{ cm}, \theta = 1.6 \times 10^{-19} \text{ c}$$

$$4) \text{Ais tan ce} = \frac{\text{moment}}{\text{charge}} = \frac{6.2 \times 10^{-3} \text{ cm}}{1.6 \times 10^{-19}} = 3.9 \times 10^{-11} \text{ m}$$

b) Calculate the Force (i)

$$i = \text{moment} \times \text{Electric field} = 6.2 \times 10^{-3} \text{ cm} \times 1.6 \times 10^{-19}$$

$$i = 9.3 \times 10^{-26} \text{ NM}$$

5) $r = 0.5 \text{ m}$, $E = 2.0 \text{ N/C}$. calculate Q

$$E \frac{KQ}{r^2} = \frac{Er^2}{K} = \frac{2 \times 0.5^2}{9 \times 10^9} = 5.56 \times 10^{-10} \text{ c}$$

Note: $1 \text{ v} = 1 \text{ J/c} = 1 \text{ NM/C}$

$$1 \text{ v/m} = 1 \text{ N/C}$$

CHAPTER THREE EXERCISES

1) Energy density $\mu = 2.5\text{J}, v=1.00\text{m}^3$

$$\frac{E}{V} = \frac{1}{2} E_0 E^2$$

$$U = \frac{2.5}{1} = 2.5\text{J} / \text{m}^3$$

$$E = \sqrt{\frac{2\mu}{\epsilon_0}} = \sqrt{\frac{2 \times 2.5\text{J} / \text{m}^3}{8.85 \times 10^{-12}}}$$

$$E = 7.52 \times 10^5 \text{ V/m}$$

$$\frac{u_1}{E_1^2} = \frac{u_2}{E_2^2}$$

$$u_2 = \frac{E_2^2 \times u_1}{E_1^2}$$

$$E_2 = \frac{1}{4} E_1$$

$$= \frac{\left(\frac{1}{4} E_1\right)^2 \times 2.5}{E_1^2}$$

$$E_2 = 0.2 \text{ J/M}^3$$

3). $Q_1^{0.1\text{m}} \text{-----} Q_2^{0.5\text{m}} \text{-----} Q_3$

Taking Q_3 as the test charge

$$\frac{KQ_1Q_2}{r_{13}} + \frac{KQ_2Q_3}{r_{13}} = KQ_3 \left[\frac{Q_1}{r_{13}} + \frac{Q_2}{r_{23}} \right]$$

$$w.d = 9 \times 10^9 \times 1.5 \times 10^{-6} \left[\frac{3 \times 10^{-6}}{1} + \frac{2 \times 10^{-6}}{0.5} \right] = 9.5 \times 10^{-2} \text{ J}$$

4). The final kinetic Energy K.E

$$K.E = \frac{KQ_1Q_2}{r_{12}} + W.D = \frac{9.0 \times 10^9 \times 3 \times 2 \times 10^{-12} + 9.5 \times 10^{-2}}{0.5}$$

$$K.E = 2.0 \times 10^{-1} \text{ J}$$

CHAPTER FOUR EXERCISES

Shortcut; $\theta = \theta/E_0 = E_0 = 8.85 \times 10^{-12} \text{ NM}^2/\text{c}$

1) $\theta = \frac{\theta}{E_0} = \frac{3 \times 1.6 \times 10^{-19}}{8.85 \times 10^{-12}} = 5.43 \times 10^{-8} \text{ NM}^2/\text{c}$

2) Same procedure

$$\theta = \frac{\theta}{E_0} = \frac{5 \times 10^{-6}}{8.85 \times 10^{-12}} = 5.6 \times 10^5 \text{ NM}^2/\text{c}$$

3) INFINITE LINE

$$\lambda = 184 \text{ c/cm} = 18 \times 10^{-6} \times 100 = 18 \times 10^{-4} \text{ c/m}$$

4) $Q = \frac{Q}{E_0} = \frac{4.8 \times 10^{-6}}{8.85 \times 10^{-12}} = 5.42 \times 10^5 \text{ NM}^2/\text{c}$

CHAPTER SIX EXERCISES

$A = 200 \text{ cm}^2 = 0.02 \text{ m}^2$, $d = 4 \times 10^{-3} \text{ m}$, $V = 500 \text{ v}$.

Find Q

$$Q = cv = \frac{E \cdot A}{d} \times V = \frac{0.02 \times 8.85 \times 10^{-12}}{4 \times 10^{-3}} \times 500 = 2.2 \times 10^{-8} \text{ c.}$$

$$Q = 22 \text{ nc}$$

2). $V = V_{\text{max}}/2$ from question $V_{\text{max}} = 2v$

$$Q = cv \dots V = \frac{Q}{c} = \frac{Qd}{AE_0}$$

$$V_{\text{max}} = \frac{2Qd}{AE_0} \dots \text{but } E = \frac{V_{\text{max}}}{d} \implies E = \frac{2Qd}{AE_0 \times d} = \frac{2Q}{AE_0}$$

$$E = \frac{2 \times 10 \times 10^{-8}}{4.84 \times 10^{-4} \times 6 \times 8.85 \times 10^{-12}} = 7.85 \times 10^8 \text{ v/m}$$

3). $K = \frac{c}{c_0} = \frac{0.482 \mu\text{f}}{0.2 \mu\text{f}} = 2.41$

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4). $A = 2000 \text{ cm}^2 = 0.02\text{m}^2$. $E_0 = 8.85 \text{ mo}^{-12}$, $d = 0.4\text{cm} = 0.004\text{m}$

$$C = \frac{c_0 A}{d} = \frac{8.85 \times 10^{-12} \times 0.02}{0.004} = 4.45 \times 10^{-11}, C = 44 \text{ pf}$$

5). $K = E_r = 2.6$ $V = 500\text{v}$ $d = 0.004\text{m}$.

$$Q_1 = CV = E_r \{E_0 A/d\} \times V.$$

From question (4) $E_0 A/d = 4.45 \times 10^{-11}$

$$Q_1 = 2.6 \times 4.45 \times 10^{-11} \times 500$$

(presence of dielectric)----- 5.73×10^{-8}

But in (4) above, dielectric is absent

$$Q_0 = CV = 500 \times 4.45 \times 10^{-11}, Q_0 = 2.2 \times 10^{-8} \text{C}$$

$$Q_3 = Q_1 - Q_0 = (5.72 - 2.2) \times 10^{-8}$$

$$Q_3 = 3.52 \times 10^{-8} \quad Q_3 = 35 \text{nc (change due to dielectric)}$$

6). $E = \frac{1}{2} CV^2 = \frac{1}{2} \times 1.2 \times 10^{-6} \times (3000)^2 = 5.4 \text{ joules}$

7). Width = 0.5m, L = ? $d = 0.2 \times 10^{-4} \text{m}$ $C = 4 \times 10^{-6}$. $E_r = 2.8$

$$C = \frac{E_0 E_r A}{d} \quad (\text{find A to get L})$$

$$A = \frac{cd}{E_0 E_r} = \frac{4 \times 10^{-6} \times 0.2 \times 10^{-4}}{2.8 \times 8.85 \times 10^{-12}}$$

$A = 3.2284 \text{m}^2$ But $A = L \times W = L = \frac{A}{W} = \frac{3.2284 \text{m}^2}{0.5 \text{m}} = L = 6.456 \text{m}$

8). Note charging $= q = CE(I - e^{-t/Rc})$

Discharging

$$Q_1 = Q_0 e^{-t/Rc} \quad \text{Redischarges}$$

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$$I = \frac{dQ}{dt} = \frac{Q_0}{RC} e^{-t/RC}$$

In the question above

Remaining charge = I- decay charged

$$I - \frac{2}{5} = \frac{3}{5} Q_0$$

$$Q_1 = Q_0 e^{-t/RC}$$

$$\frac{3}{5} Q_0 = Q_0 e^{-\frac{t}{600 \times 10^{-6} \times 100000}}$$

$$\ln\left(\frac{3}{5}\right) = \frac{-t}{600 \times 10^{-6} \times 100000}$$

$$t = -\ln\left(\frac{3}{5}\right) \times 600 \times 10^{-6} \times 100000$$

$$t = 30.65 \text{ sec}$$

9). Energy = $\frac{1}{2} Qv$

$$Q = ? \quad V = 12v$$

$$E = 5.4 \times 10^{-3} J$$

$$Q = \frac{2E}{v} = \frac{2 \times 5.4 \times 10^{-3}}{12} \\ = 9 \times 10^{-4} C$$

10). Refer to your textbook for diagram

C_2 $C_7 = \frac{1}{4} + \frac{1}{8}$ because C_2 and C_7 are in series

$$C_{2,7} = \frac{4 \times 8}{4 + 8} = \frac{32}{12} = \frac{8}{3}$$

Also

C_1, C_4, C_5, C_6 and $C_{2,7}$ are in parallel

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$$C_{145627} = C_1 + C_4 + C_5 + C_6 + C_{2,7}$$

$$= 4 + 4 + 6 + 2 + 8/3$$

$$= 56/3 \mu\text{f}$$

$5 \mu\text{f}$ and the combining equivalent of C_1, C_4, C_5, C_6 and $C_{2,7}$ are in parallel

$$\frac{1}{C_{\text{equ}}} = \frac{1}{C_3} + \frac{1}{C_{145627}}$$

$$\frac{1}{C_{\text{equ}}} = \frac{1}{5} + \frac{1}{56/3} = \frac{1}{5} + \frac{3}{56}$$

$$C_{\text{equ}} = \frac{56 \times 5}{15 + 56} = 3.943 \mu\text{f}$$

11). $C_1 = 2 \mu\text{f}$

$Q = Cv$ note different charge is stored in as much they have different capacitor of capacitance but the same voltage across them

$$Q_1 = C_1 V$$

$$= 2 \times 10^{-6} \times 500$$

$$= 1 \times 10^{-3} \text{c}$$

12). The above question is the definition of electric potential which is the work done in taken a charge from one place to another.

$$V = kq/r = r = 6 \text{cm} = 0.06 \text{m}$$

$$Q = 1.2 \times 10^{-6} \text{c}$$

$$\frac{9 \times 10^9 \times 1.2 \times 10^{-6}}{0.06} = 180 \text{kv}$$

13). $Q = 1.0 \times 10^{-6} \text{c}$

$$C_1 = 0.001 \times 10^{-6} \text{f}, C_2 = ?$$

$$d_1 = d \quad d_2 = 1/2d$$

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$$A_1 = A \quad A_2 = 3A$$

$$C = \frac{E_0 A}{d} \dots \frac{cd}{A} = K$$

$$\frac{C_1 d_1}{A_1} = \frac{C_2 d_2}{A_2}$$

$$C_2 = \frac{C_1 d_1 A_2}{A_1 d_2} = \frac{1.0 \times 10^{-6} \times d \times 3A}{A \times \frac{1}{2} d}$$

$$C_2 = 6C_1 = 6 \times 0.001 \times 10^{-6} \text{ f} \\ = 6 \text{ nf}$$

$$Q = CV$$

$$V = \frac{Q}{C} = \frac{1 \times 10^{-6}}{1 \times 10^{-6} \text{ c}}$$

$$\text{Potidiff } V = 1000 \text{ v}$$

14). Power = 75 w = p

$$t = 15 \text{ minutes} = 15 \times 60 = 900 \text{ sec}$$

$$v = 150 \text{ v}$$

$$\text{work} = \text{power} \times \text{time} = \frac{1}{2} CV^2$$

$$C = \frac{\text{power} \times \text{time}}{\frac{1}{2} v^2} = \frac{75 \times 900}{\frac{1}{2} (150)^2}$$

$$C = 6 \text{ f}$$

15). $V = 500 \text{ v}$, $A = 0.1 \text{ m}^2$, $d = 0.001 \text{ m}$

$$E_0 = 8.85 \times 10^{-12} \text{ f/m. } Q = ?$$

$$\frac{VAE_0}{d} = 5000 \times 0.1 \times 3.85 \times 10^{18}$$

Note ----- Q =

$$Q = 4.425 \times 10^{-6} \text{ C} \text{ ----- } Q = 7.44 \text{ C}$$

CHAPTER 9 (SUPPLIMENTARY PROBLEMS)

- 1) $H^{2+} = 2e$
 $F = ? \quad v = 2 \times 10^5 \text{ ms}^{-1}$
 $B = 0.75 \text{ T}$
 $q = 2e = 2 \times 1.6 \times 10^{-19} \text{ C}$
 $f = qvB = 2 \times 1.6 \times 10^{-19} \times 2 \times 10^5 \times 0.75$
 force $F = 4.8 \times 10^{-14} \text{ N}$

- 2) $m_{\text{proton}} = 1.67 \times 10^{-27}$
 $B = 0.60 \text{ T} \quad q = 1.6 \times 10^{-19}$
 Charge of proton.
 Note $\frac{1}{2} Mv^2 = \text{Energy} = \frac{1}{2} m^2 v^2 / m$
 $m^2 v^2 = q^2 B^2 r^2$ (if $MV = qBv$)

$$\frac{1}{2} mv^2 = \frac{\frac{1}{2} q^2 B^2 r^2}{m} = \frac{1}{2} \frac{m^2 v^2}{m}$$

$$\frac{1}{2} \times \frac{(1.6 \times 10^{-19} \times 0.60 \times 0.012)^2}{1.67 \times 10^{-27}}$$

$$= 3.9733 \times 10^{-16} \text{ J in electron volt}$$

$$\text{Lev. ----- } 1.6 \times 10^{-19} \text{ J}$$

$$\text{Work Wer ----- } \left(\frac{3.9733 \times 10^{-16} \text{ J} \times \text{lev}}{1.6 \times 10^{-19}} \right)$$

$$= 2483 \text{ ev} = 2480 \text{ ev.}$$

9.3 $B = 0.1 + 0.3j - 0.2k$ (in tesla)

$$F = qv B \sin \theta$$

$$I(0) - \begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ 3.2 \times 10.5 & 0 & 0 \\ 0.1 & 0.3 & -0.2 \end{vmatrix} \begin{matrix} \mathbf{j}(-64000) + \mathbf{k}(96000) \\ = 64000\mathbf{i} + 96000\mathbf{k} \end{matrix}$$

$$(v \times B) = \sqrt{64000^2 + (96000)^2}$$

$$= 115,377.64$$

$$F = q(V \times B) = 1.6 \times 10^{-19} \times 115,377.64$$

$$F = 1.8 \times 10^{-14} \text{N}$$

$$9.4 \quad f = Ma - qvB = \frac{MV^2}{r}$$

$$r = \frac{MV^2}{QVB} = r = \frac{V_{RM}}{QB}$$

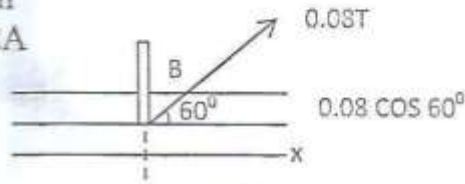
$$\frac{1}{2}MV^2 = ev_0, V = \frac{\sqrt{2e}v_0}{m} = \frac{\sqrt{2 \times 1.6 \times 600 \times 10^{-19}}}{1.16 \times 10^{-26}}$$

$$V = 128653.5042 \text{m/s}$$

$$1 = \frac{VM}{QB} = \frac{128653.5042 \times 1.16 \times 10^{-26}}{1.6 \times 10^{-19} \times 0.6} = 0.0155 \text{M}$$

$$= r = 0.016 \text{m}$$

$$9.5 \quad I = 2 \text{A}$$



$L \times B$				wires
$I(0) -$	I	J	K	$J(0) + k(1.5 \times 0.0069)$
$L \times b$	1.5	0	0	$= 0.1035k$
But f	0.04	0.069	0	$= L \times B = I L B \sin \theta$
$= 2 \times$				$0.1035k = 0.2In$

In the z direction or (k direction)

$$9.6 \quad b = 0.12 \text{T}, N = 60 \text{turn}, r = 0.013 \text{m},$$

$$A = \pi r^2 = 5.3 \times 10^{-4} \text{m}^2$$

$$I = 1.5 \text{A}, \theta = 90^\circ$$

$$Y = BINA \sin \theta$$

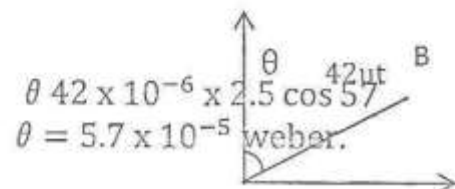
$$= 0.12 \times 1.5 \times 60 \times 5.3 \times 10^{-4} \sin 90$$

$$\text{Torque } T = 5.72 \times 10^{-3}$$

$$F_1 = \frac{2 \times \text{Torque}}{\text{radius}} = 0.88 \text{N}$$

$$9.7) \quad B = 42 \times 10^{-6} \text{T}, \theta = 57^\circ, A = 2.5 \text{m}^2$$

$$\theta = BA \cos \theta$$



CHAPTER 11

- 1) From ground state the $n =$ excited state

$$E_{11} = \frac{-13.6\text{ev}}{4^2} = \frac{-13.6\text{ev}}{16} = -0.85\text{ev}$$

$$E_1 = \frac{-13.6\text{ev}}{12} = \frac{-13.6\text{ev}}{12} = -13.6\text{ev}$$

$$\Delta E = E_4 - E_1 = (-0.85 + 13.6)\text{ev}$$

$$\Delta E = 12.75\text{ev}$$

- 2) Speed of an e^- in the 2nd orbit

$$V = \frac{nl}{2\lambda mr} = \frac{2 \times 6.6 \times 10^{-34}}{2\lambda \times 9.11 \times 10^{-31} \times 0.0529 \times 4}$$

$$\text{Note: } r = 0.0529n^2 \text{ and } M_e = 9.11 \times 10^{-31} \text{kg}$$

$$v = 1.095 \times 10^3 \text{Mls}$$

- 3) Calculate freq from $n = 2$ to $n = 5$

$$E_2 = \frac{-13.6}{2^2} = \frac{-13.6}{4} = -3.4$$

$$E_5 = \frac{-13.6}{5^2} = \frac{-13.6}{25} = -0.544$$

$$\Delta E = E_5 - E_2 = 0.544 + 3.4 = 2.856\text{ev}$$

$$E = hf, \quad f = \frac{E}{h}$$

$$F = \frac{2.856 \times 1.6 \times 10^{-19}}{6.651 \times 10^{-34}} = 6.68 \times 10^{14} \text{hz}$$

- 4) From D_2 to n_{0-1}

$$E_2 = \frac{-13.6}{2^2} = -3.4$$

$$E_{0,1} = \frac{-13.6}{0} = 0$$

$$\Delta E = 0 - (-3.4) = 3.4\text{ev}$$

$$E = hf, \quad f = \frac{E}{h}$$

$$F = \frac{3.4 \times 1.6 \times 10^{-19}}{6.639 \times 10^{-34}} = 8.2 \times 10^{14} \text{Hz}$$

- 5) $F = 98.9\text{MHz} = 98.9 \times 10^6 \text{Hz}$

$$P = 750 \times 10^3 \text{W}$$

Calculate the no of photons for seconds

$$E = pt = 750 \times 10^3 \times 1 = 75.0 \times 10^3 \text{J}$$

$$E = nhf, \quad n = \frac{E}{hf} = \frac{75.0 \times 10^3}{6.654 \times 10^{-34} \times 98.9 \times 10^6}$$

$$n = 1.14 \times 10^{31} \text{photons}$$

CHAPTER 13

1) Half life of iodine $t_{1/2} = 8$ days at a certain time, $N = 4 \times 10^4$ nuclei

a) Calculate the activity

As stated earlier, Activity $A = \lambda N$

$$\lambda = \frac{0.693}{t_{1/2}}$$

converting $t_{1/2}$ to seconds

$$t_{1/2} = 8 \times 86400 = 691200 \text{ s}$$

$$\lambda = \frac{0.693}{691200} = 1.00 \times 10^{-6} \text{ s}^{-1}$$

$$A = 1.00 \times 10^{-6} \times 4 \times 10^4 = 4.0 \times 10^8 \text{ dec}$$

b) Using $\frac{N}{N_0} = 2^{-n} \quad n = \frac{t}{t_{1/2}} = \frac{1 \times 864}{8 \times 864} = \frac{1}{8}$

note (How many iodine remained after 1 day)

(hence $t = 1 \text{ day} = 1 \times 86400$)

$$N = N_0 (2^{-n})$$

$$N = 4 \times 10^{14} (2^{-1/8}) = 3.7 \times 10^{17} \text{ nuclei}$$

2) $N_0 = 200 \quad N = 25$

Midday means 12 O clock between 12 O clock and 3 O clock $T = 3$ hours.

Using equation (1)

$$N = N_0 \left(\frac{1}{2}\right)^{t/T_{1/2}}$$

$$\left(\frac{N}{N_0}\right) = \left(\frac{1}{2}\right)^{t/T_{1/2}}$$

$$\left(\frac{25}{200}\right) = \left(\frac{1}{2}\right)^{T/T_{1/2}}$$

$$\left(\frac{1}{8}\right) = \left(\frac{1}{2}\right)^{T/T_{1/2}}$$

$$\left(\frac{1}{2}\right)^3 = \left(\frac{1}{2}\right)^{T/T_{1/2}}$$

$$3 = \frac{T}{T_{1/2}} \quad T_{1/2} = \frac{3}{3}$$

Half life $T_{1/2} = 1$ hour

3) $t = 2$ hours

$$N_0 = 8000 \quad N_{\text{died}} = 1000$$

Remaining bacteria

$$N = N_0 - N_{\text{died}}$$

$$8000 - 1000 = 7000$$

$$\left(\frac{N}{N_0}\right) = \left(\frac{1}{2}\right)^{t/T_{1/2}}$$

$$\frac{7000}{8000} = \left(\frac{1}{2}\right)^{t/T_{1/2}}$$

$$\frac{7}{8} = \left(\frac{1}{2}\right)^{t/T_{1/2}}$$

$$\frac{2}{t^{1/2}} = \frac{\log\left(\frac{7}{8}\right)}{\log\left(\frac{1}{2}\right)}$$

$$t^{1/2} = \frac{2}{\left[\frac{\log\frac{7}{8}}{\log\frac{1}{2}}\right]} = 0.19$$

$$t^{1/2} = 10.38 \text{ hour}$$

$$N = 5000 - \text{population}$$

$$\frac{5000}{8000} = \left[\frac{1}{2}\right]^{T/10.38}$$

$$\left(\frac{5}{8}\right) = \left[\frac{1}{2}\right]^{T/10.38}$$

Take log of both side we have

$$\text{Log} \left(\frac{5}{8}\right) = \frac{T}{T_{1/2}} \log\left(\frac{1}{2}\right)$$

$$T = 10.4 \log \frac{\left(\frac{5}{8}\right)}{\log\left(\frac{1}{2}\right)}$$

$$= 7 \text{ hours}$$

4) $N_1 = N_0$
 $N_{\text{died}} = 2/3 N_0$
 $\text{Remaining} = N_0 = 2/3 N_0$
 $N = 1/3 N_0$
 $N = N_0 \left(\frac{1}{2}\right)^{T/T_{1/2}}$

$$\text{Log} \left(\frac{1}{3}\right) = \log\left(\frac{1}{2}\right)^{T/T_{1/2}}$$

$$\text{Log} \left(\frac{1}{3}\right) = \frac{T}{T_{1/2}} \log \left(\frac{1}{2}\right)$$

$$T = T_{1/2} \log \frac{(1/3)}{\log(1/2)}$$
$$= 16.48 = 16.5 \text{ hours}$$

Check out this parameters:

λ = decay constant (S^{-1})

note n = no of disintegrations

N_0 = initial activity

N = after decay the remaining activity

$T_{1/2}$ = half life of a substance

Undergoing radioactive decay in see